

GNN Explainability

Shichang Zhang

11.02.2021

Roadmap

- Model Explainability
 - Motivating Examples for Images and Tabular Data
- GNN Explainability (Graph Data Explainability)
 - Graphs vs. Images vs. Tabular Data
 - SubgraphX (ICML 2021)

Model Explainability

- Goal: understand black-box models, e.g. NNs.
- Existing approaches
 - Instance-level
 - Example-specific understanding, why an input data is mapped to a certain output
 - Model-level
 - High-level generic understanding, how the model mechanism leads to a certain output

Motivating Examples: Images

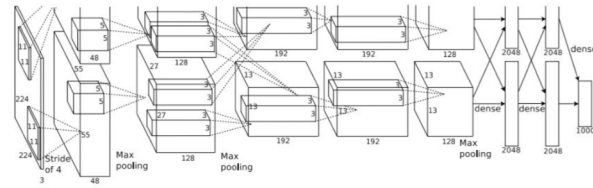
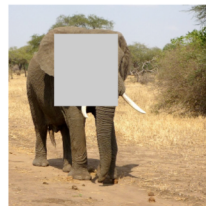
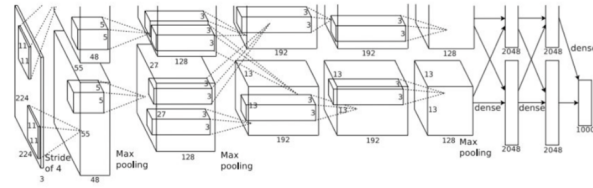
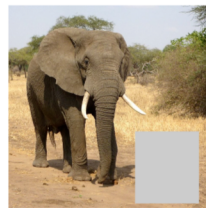
- Instance-level: Which pixels are importance for classifying an image

Motivating Examples: Images

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Which pixels matter: Saliency via Occlusion

Mask part of the image before feeding to CNN,
check how much predicted probabilities change

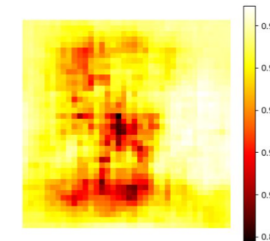
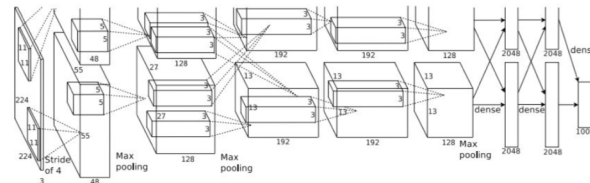
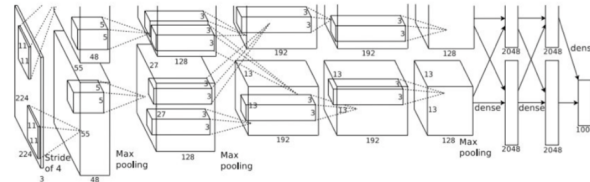
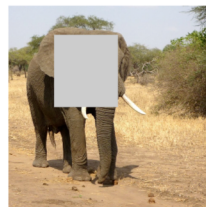
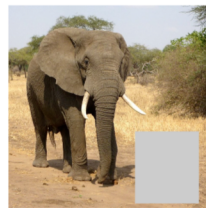


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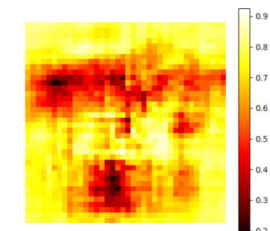
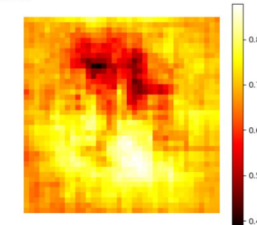
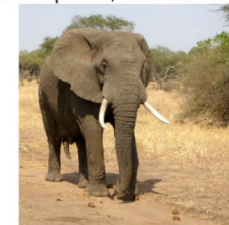
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African elephant, *Loxodonta africana*



Motivating Examples: Images

- Model-level: What kind of image maximizes the probability for a certain class

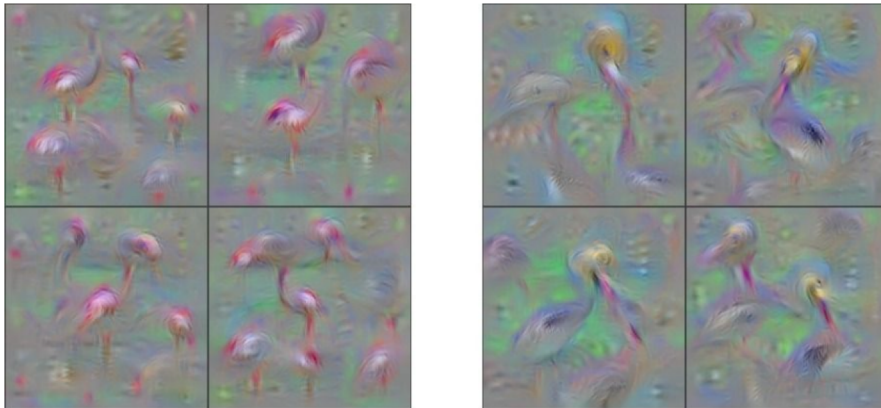
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Random Initialization



Flamingo

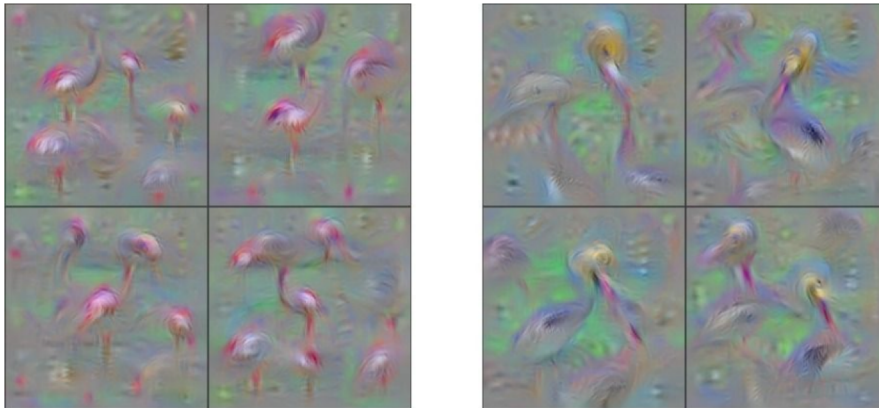
Pelican

Synthesized

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Smart Initialization considering multimodality.
The “grocery store” class



Synthesized

Ground Truth

Motivating Examples: Tabular Data

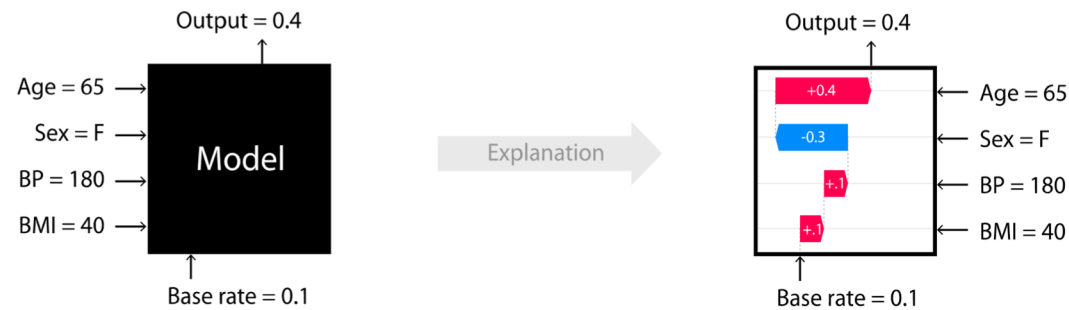
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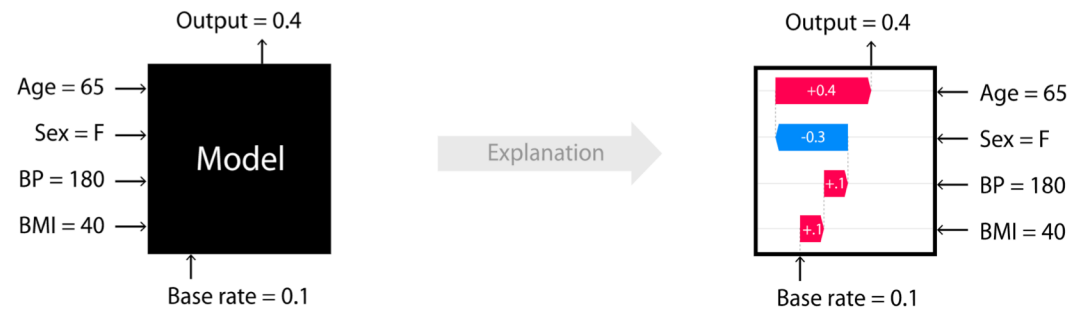
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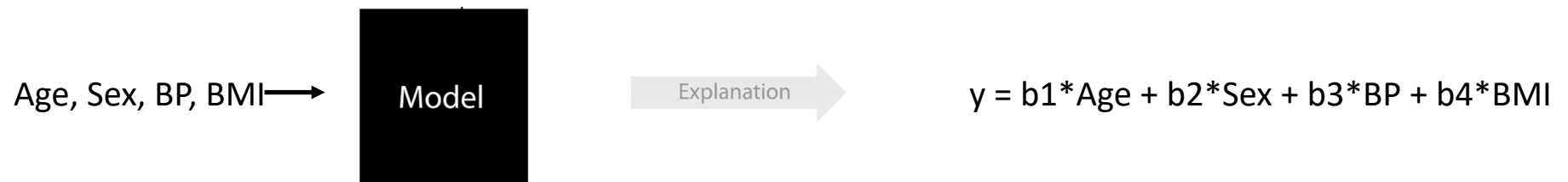


Motivating Examples: Tabular Data

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- Model-level
 - Ex. a simple linear model



GNN Explainability

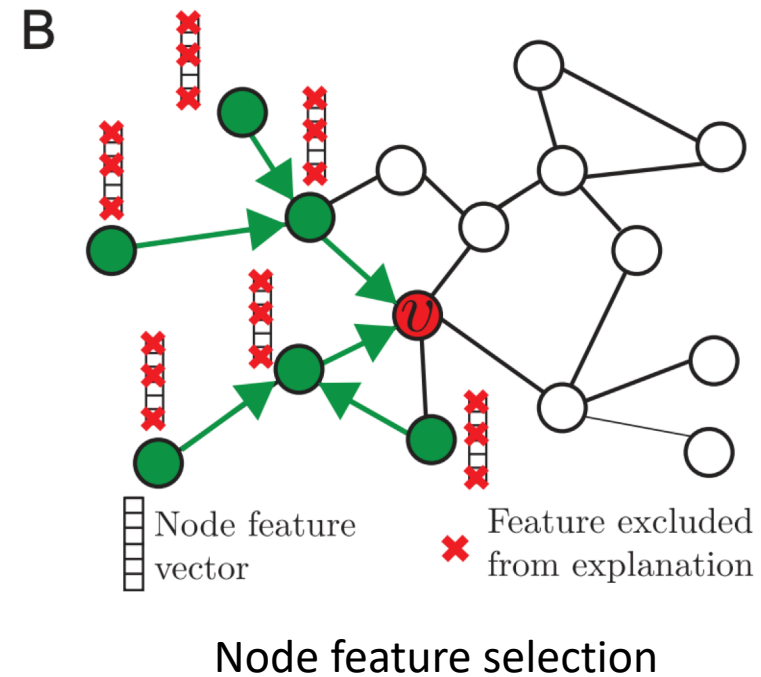
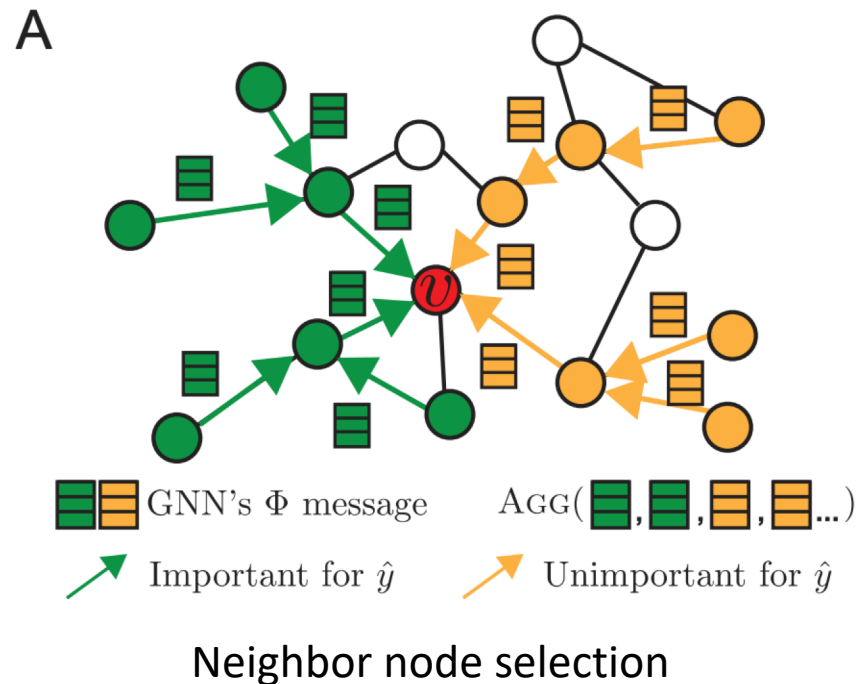
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GNN Explainability

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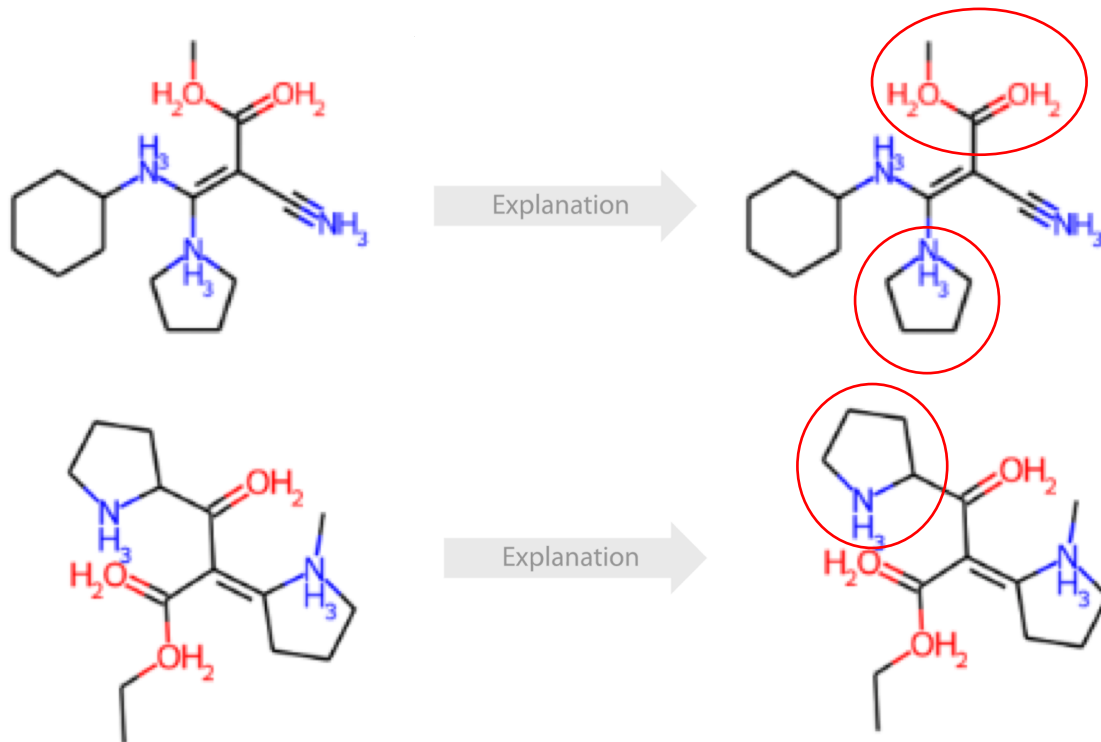


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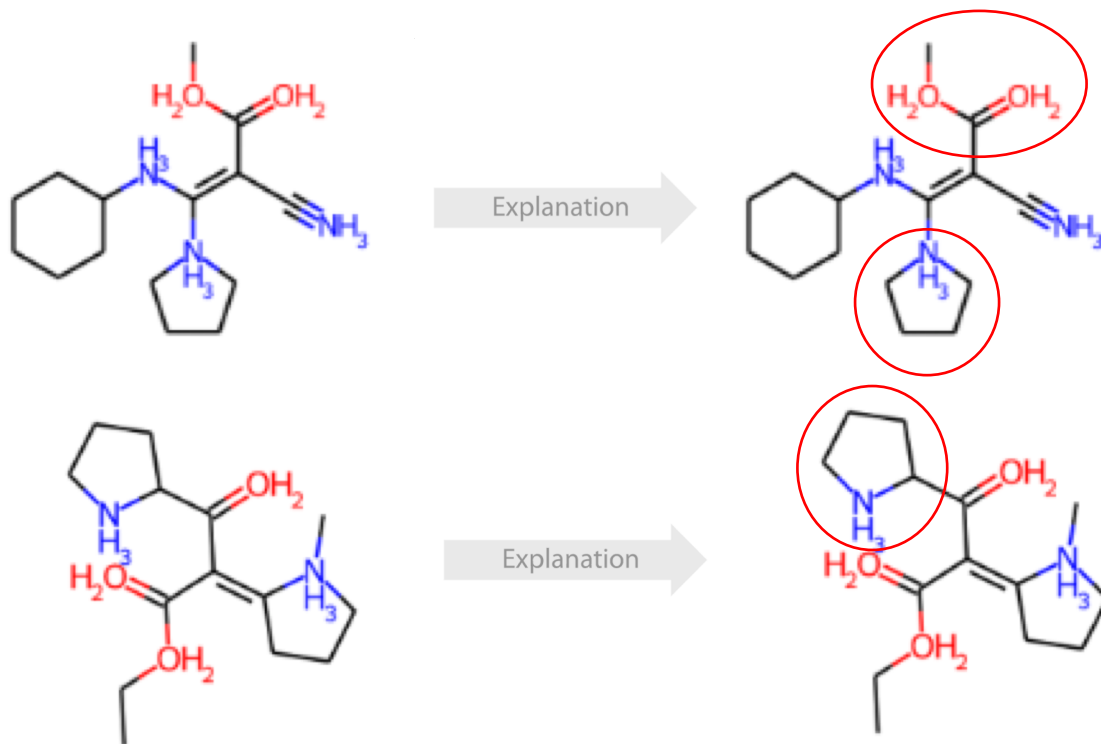
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Important subgraph selection

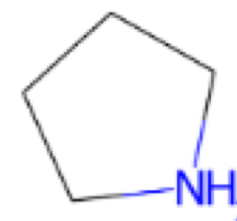
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Important subgraph selection

Model-level
(data-level)



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 - Data-level graph classification explanation is similar to frequent pattern mining.
- Explanation of graphs is more challenging than tabular data
 - Graphs as tabular data with structure information

SubgraphX (ICML21)

On Explainability of Graph Neural Networks via Subgraph Explorations

Hao Yuan¹ Haiyang Yu¹ Jie Wang² Kang Li³ Shuiwang Ji¹

- Instance level
- Graph classification

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- Goal: Identify the most important subgraph for classifying a graph

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$f(\cdot)$ GNN to be explained

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- Objective

$$\mathcal{G}^* = \underset{|\mathcal{G}_i| \leq N_{\min}}{\operatorname{argmax}} \operatorname{Score}(f(\cdot), \mathcal{G}, \mathcal{G}_i)$$

Challenges

- There are too many subgraphs. How can we explore them?
- What is a reasonable score function?

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- Variables needed for the MCTS algorithm
 - $C(\mathcal{N}_i, a_j)$ denotes the number of counts for selecting action a_j for node \mathcal{N}_i .
 - $W(\mathcal{N}_i, a_j)$ is the total reward for all (\mathcal{N}_i, a_j) visits.
 - $Q(\mathcal{N}_i, a_j) = W(\mathcal{N}_i, a_j)/C(\mathcal{N}_i, a_j)$ and denotes the averaged reward for multiple visits.
 - $R(\mathcal{N}_i, a_j)$ is the immediate reward for selecting a_j on \mathcal{N}_i ,
 $R(\mathcal{N}_i, a_j) = \text{Score}(f(\cdot), \mathcal{G}, (\mathcal{N}_i, a_j))$

Subgraph Exploration via Monte Carlo Tree Search (MCTS)

- Each MCTS iteration selects a path to a leaf node \mathcal{G}_ℓ

$$a^* = \operatorname{argmax}_{a_j} Q(\mathcal{N}_i, a_j) + U(\mathcal{N}_i, a_j),$$

$$U(\mathcal{N}_i, a_j) = \lambda R(\mathcal{N}_i, a_j) \frac{\sqrt{\sum_k C(\mathcal{N}_i, a_k)}}{1 + C(\mathcal{N}_i, a_j)},$$

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- Finally, select the subgraph with the highest reward from the leaf level

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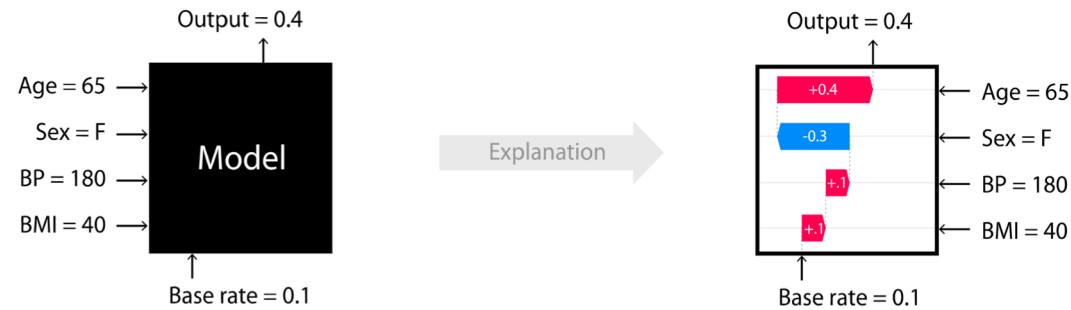
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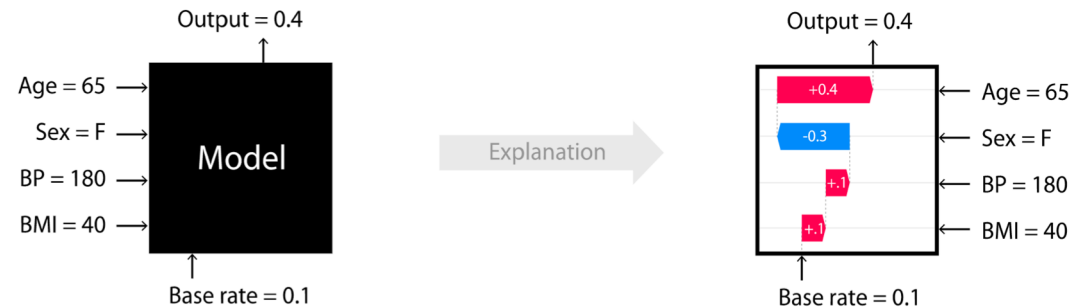
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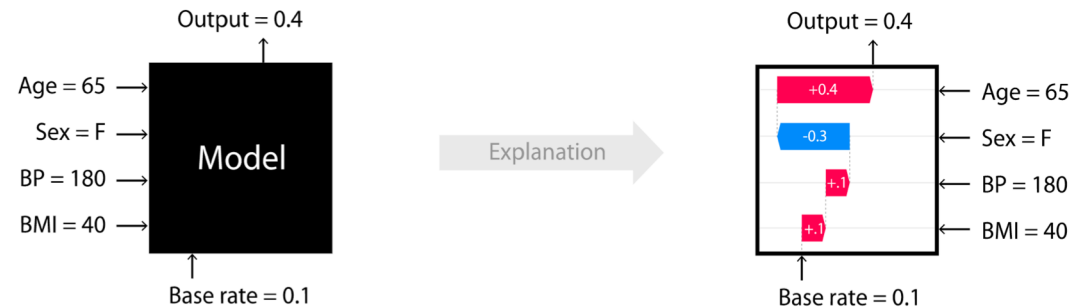
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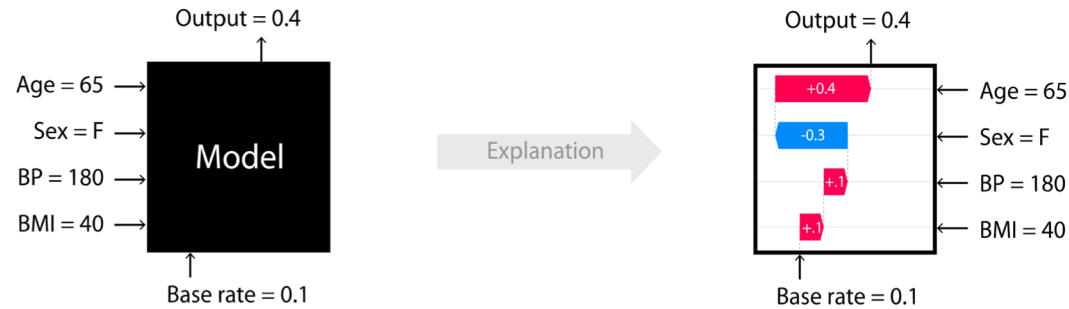
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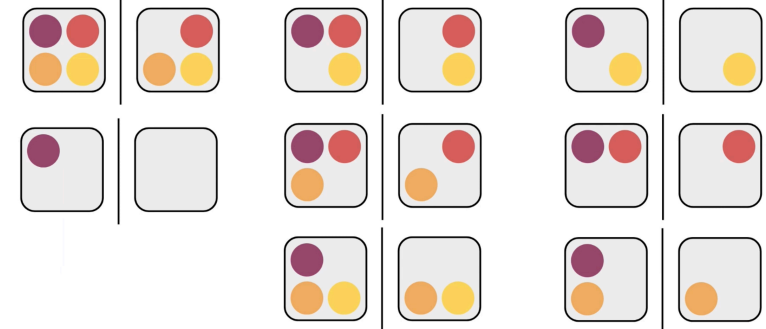


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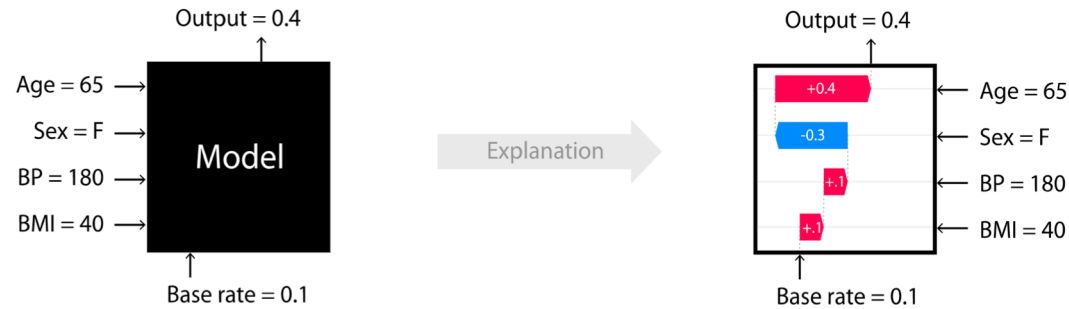
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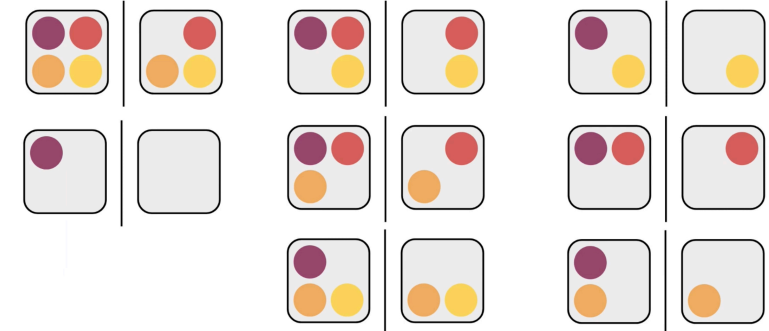
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- Shapley value:
$$I_\nu(f) = \frac{1}{|F|} \sum_{S \subseteq F \setminus \{f\}} \frac{1}{\binom{|F|-1}{|S|}} \Delta(f, S, \nu)$$

$$\Delta(f, S, \nu) = \nu(S \cup \{f\}) - \nu(\bar{S})$$

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$$F = \{\mathcal{G}_i, v_{k+1}, \dots, v_r\}$$

$$f = \mathcal{G}_i$$

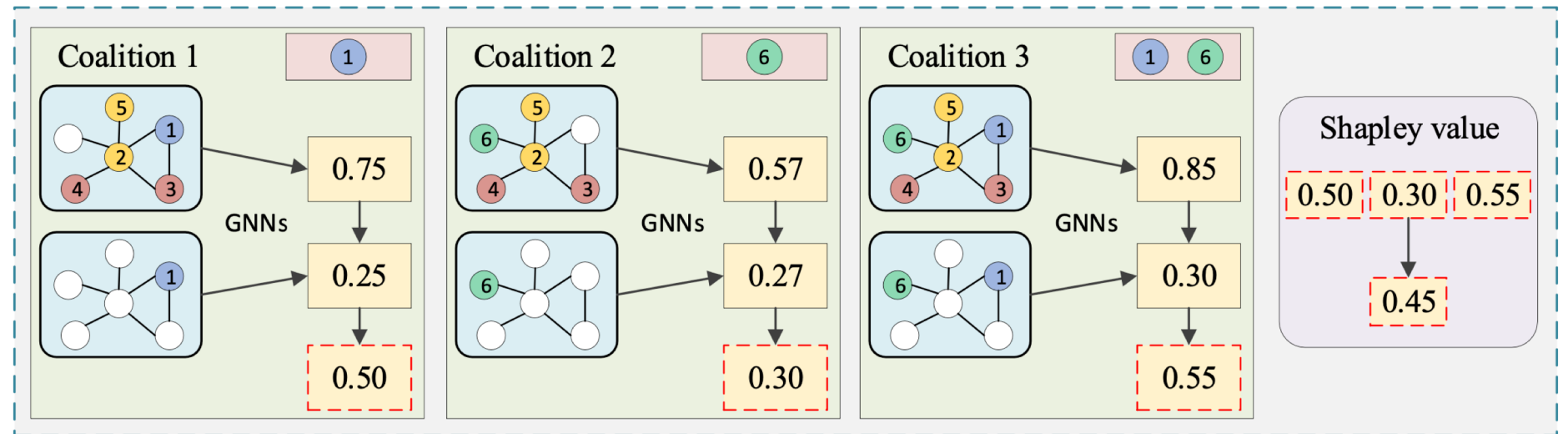
$$\nu = \text{GNN}$$

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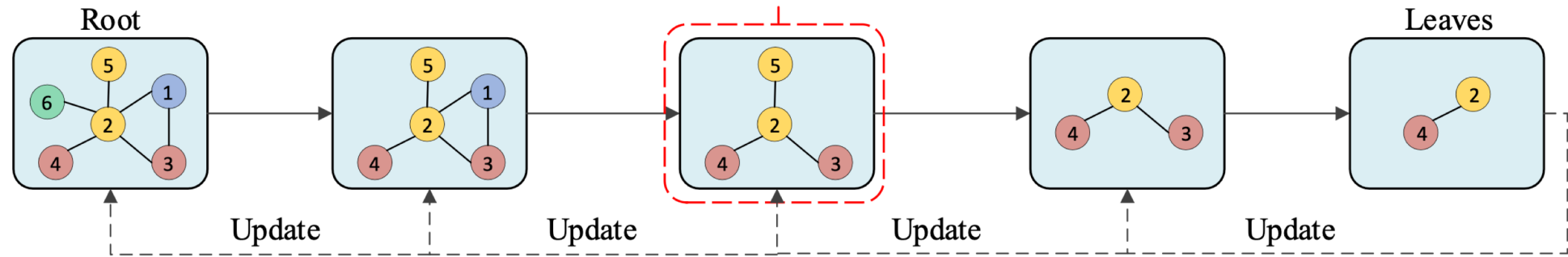
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SubgraphX Framework

Shapley Value Scoring

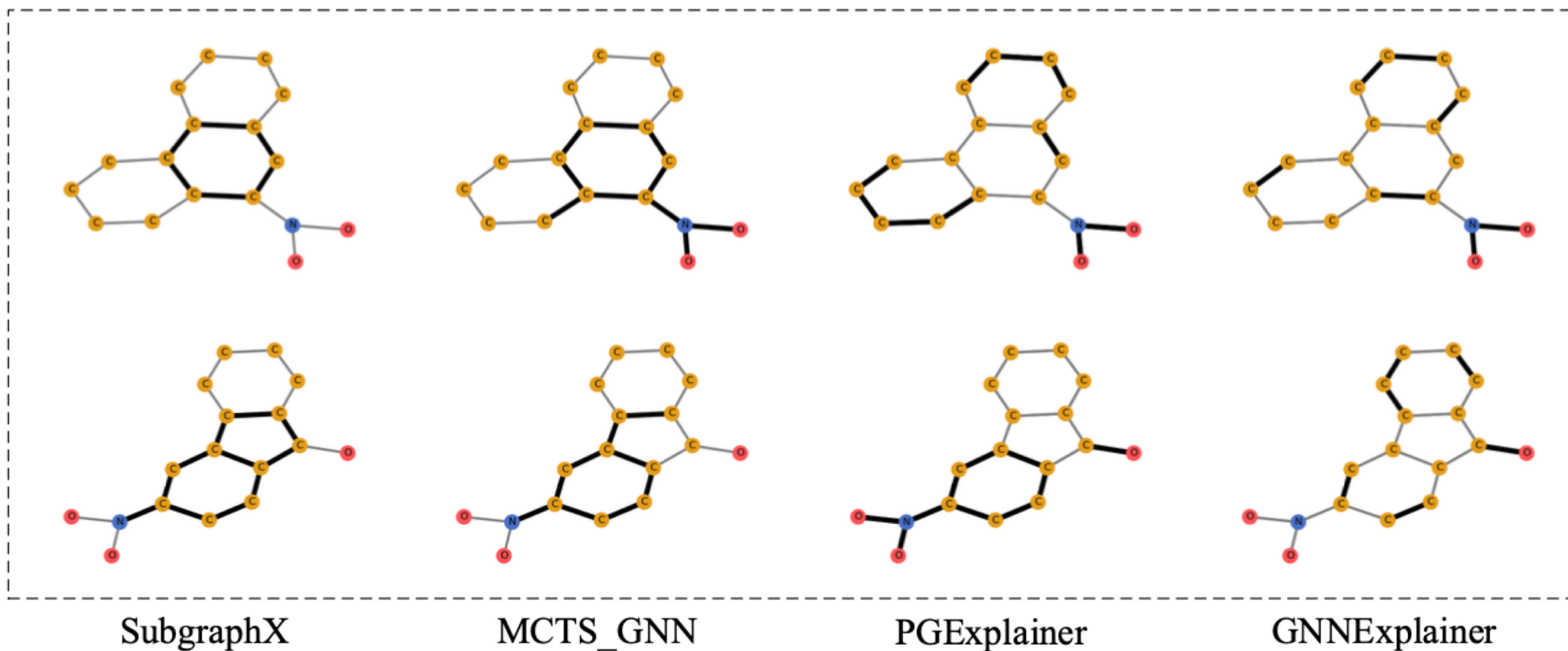


MCTS



Result Visualization

- MUTAG dataset for molecule classification



Reference

- SubgraphX: Yuan, H., Yu, H., Wang, J., Li, K., & Ji, S. (2021). On explainability of graph neural networks via subgraph explorations: <https://arxiv.org/pdf/2102.05152.pdf>
- Shapley value: <https://proceedings.neurips.cc/paper/2017/file/8a20a8621978632d76c43dfd28b67767-Paper.pdf>

Appendix